## **CAMBRIDGE INTERNATIONAL EXAMINATIONS**

**Cambridge International General Certificate of Secondary Education** 

## MARK SCHEME for the October/November 2015 series

## 0580 MATHEMATICS

0580/43 Paper 4 (Extended), maximum raw mark 130

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## **Abbreviations**

cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working

oe or equivalent SC Special Case

nfww not from wrong working

soi seen or implied

Q	uestion	Answer	Mark	Part marks
1	(a) (i)	3.9[0]	2	<b>M1</b> for 2.6 ÷ 2
	(ii)	$\frac{13}{18}$ cao	2	<b>B1</b> for any correct unsimplified fraction
	(iii)	24	3	<b>M2</b> for 9 ÷ 0.375 oe
				or <b>M1</b> for associating 9 with (100 – 62.5)%
	(b)	109 cao	3	<b>B2</b> for 108.5 to 108.6 or
				<b>M1</b> for $250 \times \left(1 - \frac{8}{100}\right)^{10}$ oe
2	(a) (i)	Image at (-2, 5), (1, 5), (1, 7)	2	<b>SC1</b> for translation $\begin{pmatrix} -4 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 4 \end{pmatrix}$
				or 3 correct vertices plotted but not joined
	(ii)	Image at $(2, -3)$ , $(5, -3)$ , $(5, -5)$	2	SC1 for a reflection in a horizontal line or in the line $x = -1$ or 3 correct vertices plotted but not joined
	<b>(b)</b>	Rotation	1	Alt
		180 oe	1	Enlargement SF $-1$ $(-1, 0)$
		(-1, 0)	1	Not as column vector
	(c) (i)	Reflection	1	
		y = -x oe	1	
	(ii)	$\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	2	SC1 for a correct row or column

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3	(a)	43 200	3	<b>M2</b> for $0.5 \times (35 + 25) \times 12 \times 120$ oe
	(b) (i)	$0.5 \times (25 + 30) \times 6 \times 120 = 19800$	M2	or M1 for $0.5 \times (35 + 25) \times 12$ oe Dep on a valid method for obtaining the width of 30 cm B1 for $0.5 \times (25 + 35)$ oe
	(ii)	45.8 or 45.83	1FT	FT for $\frac{19800}{their(\mathbf{a})} \times 100$
	(c)	1 hr 39 min	4	<b>B3</b> for 1.65 [h] or 99 mins or $\frac{33}{20}$
				or M2 for $\frac{19800}{12 \times 1000}$ oe  or M1 for $\frac{19800}{12}$ or $\frac{19800}{1000}$ or $12 \times 1000$ If zero scored then SC1 for figs 165  and  B1 for converting their time (in hours) into
	(d)	12.8 or 12.80 to 12.81	3	hours and minutes  M2 for $\sqrt[3]{\frac{19800}{3\pi}}$ or M1 for $\pi r^2 3r = 19800$
	(e)	21[.0]	2	<b>M1</b> for $\frac{19800}{1000} + 1.2$

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4	(a)	-1.5, 0.5	2	B1, B1
	(b)	Correct curve	5	B3 FT for 10 or 11 points or B2FT for 8 or 9 points or B1FT for 6 or 7 points and B1 independent for two branches  SC4 for correct curve but branches joined
	(c)	1.25 to 1.35	1	
	(d)	-1	1	
	(e) (i)	2-x	1	
	(ii)	Ruled line with gradient –1 through (0, 2) and fit for purpose  1.15 to 1.25 cao	2FT 1	<b>SC1</b> for <b>ruled</b> line, with gradient $-1$ or through $(0, 2)$ , but not $y = 2$ <b>FT</b> their $y = mx + c$ from <b>(e)(i)</b> , if $m \ne 0$ <b>SC1FT</b> for <b>ruled</b> line either with correct gradient or through $(0, c)$ , but not $y = c$
5	(a)	2180 or 2181 nfww	4	M2 for $680^2 + 2380^2 - 2 \times 680 \times 2380 \cos 65$ oe or M1 for correct implicit cosine formula  A1 for $4760000$ or $4758000$ to $4759000$
	(b)	78.7 or 78.71	3	M2 for $\frac{2380 \sin 40}{1560}$ or M1 for $\frac{1560}{\sin 40} = \frac{2380}{\sin M}$ oe
	(c)	309 or 308.7	2FT	<b>FT</b> 230 + <i>their</i> ( <b>b</b> ) <b>B1FT</b> 50 + <i>their</i> ( <b>b</b> )  for 129 or 128.7 [i.e. for <i>C</i> from <i>M</i> ]
	(d) (i)	23 39 oe	1	
	(ii)	650	2	M1 for 1560 ÷ journey time

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6	(a)	101.5625 or 102 or 101.5 to 101.6 nfww	4	<b>M1</b> for 55, 90, 110, 160 soi
				M1 for $\Sigma fm$ with frequencies and each $m$ in or on a boundary of a correct interval 2750, 2700, 4400, 6400
				<b>M1 dep on 2nd M</b> for ÷ 160
	(b)	Correct histogram drawn with correct widths and heights 1, 1.5 and 2 (no gaps)	3	B1 for each correct block If zero scored, SC1 for correct heights or frequency densities
	(c)	$\frac{40}{160}$ oe	1	
	(d) (i)	$\frac{1560}{25440}$ oe	2	<b>M1</b> for $\frac{40}{160} \times \frac{39}{159}$
	(ii)	$\frac{4000}{25440}$ oe	3	<b>M2</b> for $\frac{40}{160} \times \frac{50}{159} + \frac{50}{160} \times \frac{40}{159}$ oe
				or M1 for one of these products soi
7	(a)	83 nfww	4	<b>B3</b> for $17x = 1411$ or $17x = 14.11$ oe in form $ax = b$ or final answer of 0.83 or <b>B2</b> for $6x + 11x - 55 = 1356$ oe or $6x + 11x - [0.]$ $55 = 13[.]$ 56 or <b>M1</b> for $6x + 11(x - [0.0]5) = 13[.]$ 56
	(b)	$\frac{1}{3}$ oe nfww	4	M1 for $y(y+3)$ oe or $\frac{1}{2}(2y+1)(y+1)$ oe and B2 for $2y^2 + 6y = 2y^2 + 2y + y + 1$ oe or better or B1 for $(2y+1)(y+1) = 2y^2 + 2y + y + 1$ soi

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(c)	25 nfww	4	<b>M1</b> for $\frac{4[.]80}{w-1}$ or $\frac{7[.]80}{2w-11}$
			<b>M1</b> for $\frac{4[.]80}{w-1} = \frac{7[.]80}{2w-11}$ oe
			w-1 $2w-11M1 for 480(2w-11) = 780(w-1) oe$
			or
			ALT <b>M1</b> for $n(w-1) = 4[.]80$ or $n(2w-11) = 7[.]80$
			<b>M1</b> for $2wn - 11n = 7[.]80$
			2wn - 2n = 9[.]60 oe <b>M1</b> for $9n = 180$ oe or better
			or
			ALT <b>M1</b> for $n(w-1) = 4[.]80$ or $n(2w-11) = 7[.]80$
			<b>M1</b> for $\frac{4[.]80 + n}{n} = \frac{7[.]80 + 11n}{2n}$
			n   2n <b>M1</b> for $9n = 180$ oe or better
	1		_
(d) (i)	$\frac{1}{2}u(3u-2) = 2.5$	M1	First step must involve $\frac{1}{2}u(3u-2)$
	One further correct step leading to		
	$3u^2 - 2u - 5 = 0 \text{ with no errors}$	A1	
(ii)	(3u-5)(u+1)	2	SC1 for $(3u+a)(u+b)$
			where $ab = -5$ or $a + 3b = -2$ [a, b integers]
(iii)	29.1 or 29.05	3	$\mathbf{M2} \text{ for tan} = \frac{their \frac{5}{3}}{3 \times their \frac{5}{3} - 2}$
			or <b>M1</b> for substituting <i>their</i> positive value of $u$ into $[u \text{ and}] 3u - 2$
8 (a) (i)	Angle <i>A</i> is common to both triangles oe	1	Accept $DAB = CAB$ oe
	ADB = ABC Third angle of triangles equal oe	1dep	Dep on previous mark
(**)		_	Dop on provious mark
(ii)	Similar	1	
(iii)	8.25	2	M1 for $\frac{16}{12} = \frac{11}{BD}$ oe or better
(b) (i)	38	1	
(ii)	38	1	
(iii)	78	1	
(iv)	26	1	

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	(c)	36 nfww	5	<b>B4</b> for an equation in $m$ that simplifies to $5m = 180$ or <b>B1</b> for each of 3 of the listed angles expressed in terms of $m$ , in it's simplest form, stated or labelled on diagram Angle $PQO = m$ Angle $QOR = m$ Angle $QOR = 2m$ Angle $PQR = 3m$ or $180 - 2m$ or $90 + \frac{m}{2}$ Angle $POR = 180 - m$ or $4m$ or $360 - 6m$ Reflex angle $POR = 360 - 4m$ or $6m$ or $180 + m$
9	(a)	8	1	
	(b)	3	2	<b>B1</b> for $[g(0.5) =] 2$ soi or
				<b>M1</b> for $2\left(\frac{1}{x}\right) - 1$ or better
	(c)	$\frac{x+1}{2}$ final answer	2	M1 for $x = 2y - 1$ or $y + 1 = 2x$ or better or $\frac{y}{2} = x - \frac{1}{2}$
	(d)	4x-3	2	<b>M1</b> for $2(2x-1)-1$
	(e)	$4x^2 - 4x + 7$	2	<b>B1</b> for $\left[ \left( 2x - 1 \right)^2 \right] = 4x^2 - 2x - 2x + 1$
	<b>(f)</b>	x	1	
	(g)	$g^{-1}(x) = g(x)$	1	
	(h)	fh(x)	1	

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10	<b>A</b> -13, -20	1	
	-7n + 22 oe	2	SC1 for $-7n + k$ or $kn + 22$ oe
	$\mathbf{B} = \frac{9}{22}, \frac{10}{23}$	1	
	$\frac{n+4}{n+17}$ oe	2	<b>B1</b> for $n + 4$ oe or $n + 17$ oe seen, but not in wrong position
	C 26, 37	1	
	$n^2 + 1$ oe	1	
	<b>D</b> 162, 486	1	
	$2 \times 3^{n-1}$ oe	2	SC1 for $k \times 3^{n+p}$ [k, p integers]
			Accept $2 \times \frac{3^n}{3}$